

# A Bayesian Bandit Approach to Adaptive Delay-based Congestion Control

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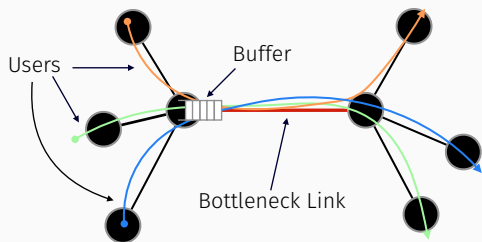
S. D'Aronco and P. Frossard

Packet Video '18, Amsterdam

Signal Processing Laboratory (LTS4)



# Congestion Control Background



- $N$  users share a network link
- $x_n$  : sending rate of user  $n$
- $u_n(x_n)$  : utility of user  $n$
- $C$  : capacity of bottleneck link / buffer draining rate

**Goal:** Maximize overall utility subject to capacity constraints

**loss-based CC** adapts the rate according to the experienced losses

**delay-based CC** adapts the rate according to the experienced delay

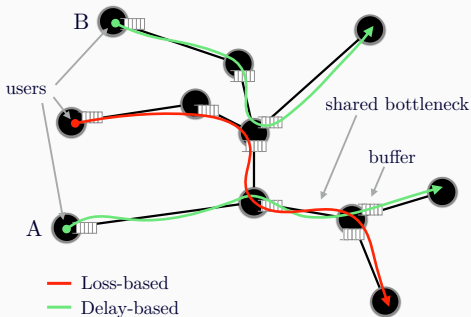
# Delay Sensitive Applications

Delay sensitive applications (e.g., VoIP applications) aim at operating at low delay, therefore they must use a delay-based congestion control algorithm.

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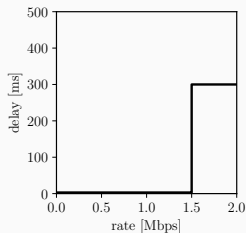
However, delay-based algorithms suffer when competing against loss-based ones (e.g., TCP)



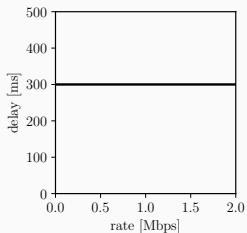
# Rate-Delay Tradeoff for Delay-based CC

single link with capacity  $C$  and buffer size  $Q_{\text{MAX}}$

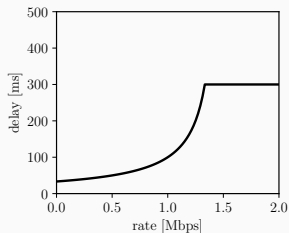
Single User



vs Loss-based



vs Delay-based



Which equilibrium point should be picked?

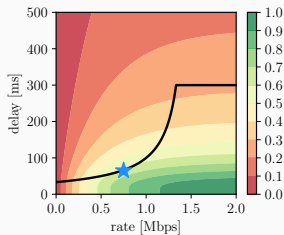
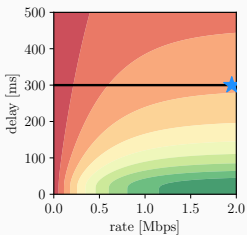
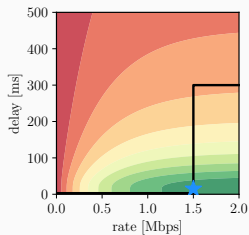
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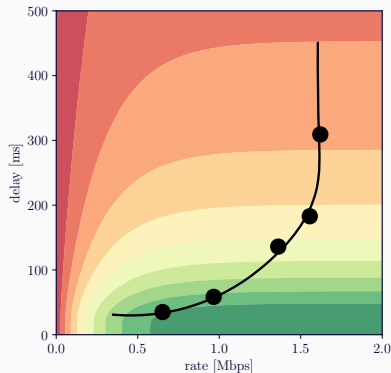
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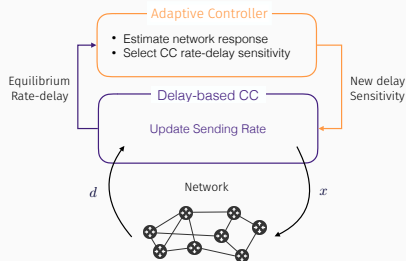
- define utility to model the communication:  $u(x, d)$
- pick the equilibrium point that maximizes this metric

# Network Sensing



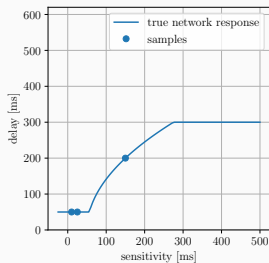
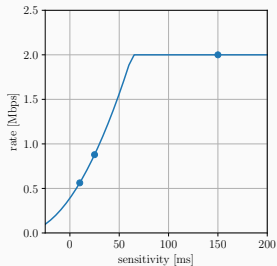
How to sense the network:

- fix sending rate – **might degrade network service**
- fix delay at equilibrium – **might degrade user satisfaction**
- fix rate-delay sensitivity by discounting the experience delay by  $d_{bl}$  – **good tradeoff**



# Network Response Model

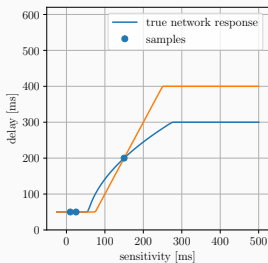
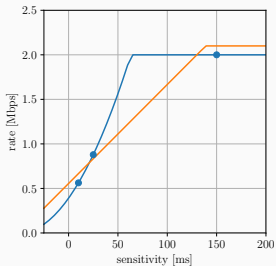
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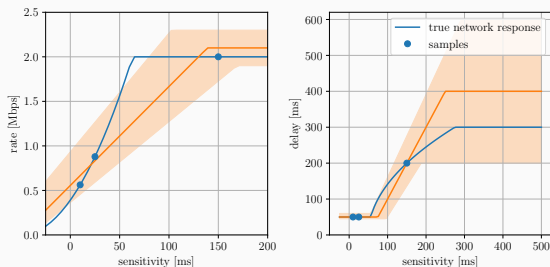


$$x_{\text{eq}} = \min(\theta_x^m d_{\text{bl}} + \theta_x^q, \theta_x^U)$$

$$d_{\text{eq}} = \max(\theta_d^L, \min(\theta_d^m d_{\text{bl}} + \theta_d^q, \theta_d^U))$$

# Network Response Model

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By assuming a prior belief on the parameters  $\theta_x$  (and  $\theta_d$ ) after observing an equilibrium point, we can infer the posterior belief

$$p(\theta | x_{\text{obs}}, d_{\text{bl}})$$

# Bandit Problem

$$\underset{d_{bl}}{\text{maximize}} \quad u(x_{eq}(d_{bl}; \boldsymbol{\theta}_x), d_{eq}(d_{bl}; \boldsymbol{\theta}_d))$$

if we know  $\theta$

# Bandit Problem

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for a single step

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$$\text{maximize}_{\pi} \mathbb{E}_p(\{x_{\text{obs}}^t, d_{\text{obs}}^t\} | \{\pi(p^t(\boldsymbol{\theta}))\}) \left[ \sum_{t=0}^{\infty} \gamma^t \mathcal{U}(\pi(p^t(\boldsymbol{\theta})), p^t(\boldsymbol{\theta})) \right]$$

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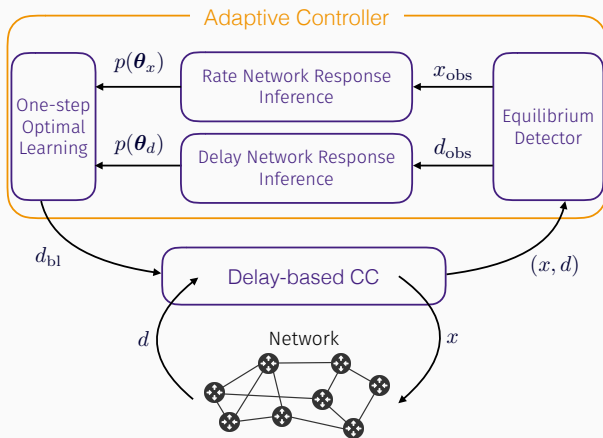
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## Receding horizon approximation

look one step ahead in the future:

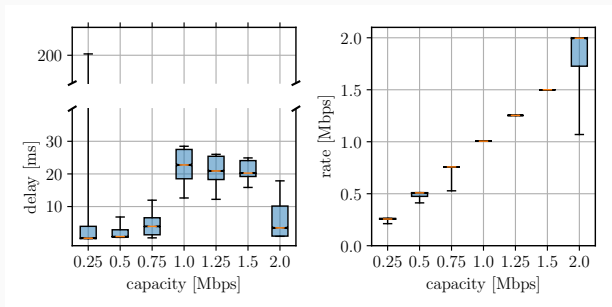
$$\underset{d_{bl}^t}{\text{maximize}} \quad \mathcal{U}(d_{bl}^t, p^t(\boldsymbol{\theta})) + \frac{\gamma}{1-\gamma} \mathbb{E}_{p^t(x_{obs}, d_{obs} | d_{bl}^t)} [\mathcal{U}^*(p^t(\boldsymbol{\theta}) | x_{obs}^t, d_{obs}^t, d_{bl}^t)]$$

# Implementation



# Results - I

Single user scenario – self inflicted delay for different values of capacity  $C$

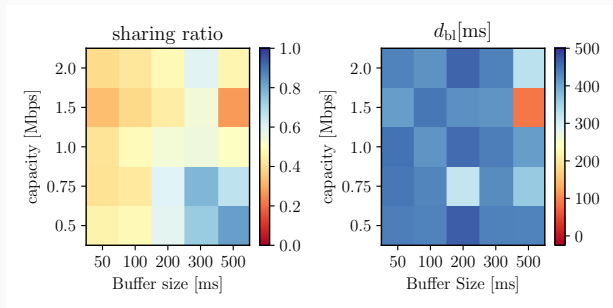


the proposed method is able to achieve a low self-inflicted delay for wide range of capacity values



## Results - II

Competing against a TCP flow - sharing ratio for different values of capacity  $C$  and buffer size  $Q_{MAX}$



the proposed method can reach a fair rate allocation in all the different scenarios

# Conclusions

## Main advantages:

- model explicitly the communication utility
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- model explicitly the communication utility
- estimate a "global" network response
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## Future directions/open problems:

- investigate performance in more complex network/scenarios
- investigate theoretical guarantees regarding equilibrium point

# Questions?

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